

Figure 3.2: The graph  $G_{\mathcal{R}}$  for rule list  $\mathcal{R}$  in Table 3.2.

Table 3.3: Rewriting a non-included rule  $r_3$  to  $r'_3$  and  $r''_3$ .

Filter $\mathcal{R}$	
$r_3$	* 0 0 0 1 *
$r_4$	0 * * 0 1 *

Filter $\mathcal{R}'$	
$r'_3$	0 0 0 0 1 *
$r''_3$	1 0 0 0 1 *
$r_4$	0 * * 0 1 *

The mean values of 10 trials are shown in Fig. 3.3. Clearly, the proposed method decreased the latency compared with the SGM [77] and SWBP [61] in all cases. In particular, the difference in latency between SGM and the proposed algorithm with 4000 and 5000 rule is greater than that with 1000 and 2000. Thus, the greater the number of rules, the more efficient the proposed algorithm becomes.

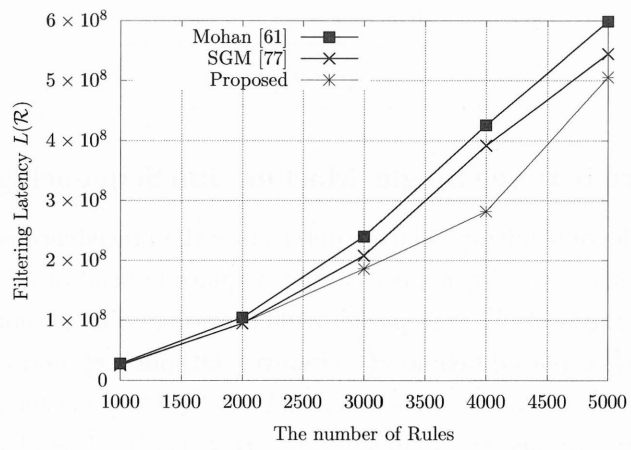


Figure 3.3: Latency of the proposed method, SGM [77], and the SWBP [61].

Table 3.4: Example of a rule list.

Filter $\mathcal{R}$	$ E(\mathcal{R}, i) _{\mathcal{U}}$
$r_1^P = * 0 * 1$	4
$r_2^P = 0 0 0 0$	1
$r_3^P = 0 * 0 0$	1
$r_4^D = 0 * 1 *$	3
$r_5^P = * 1 * 1$	3
$r_6^P = * * * 1$	0
$r_7^D = * * * *$	4
$L(\mathcal{R}, \mathcal{U}) = 60$	

### 3.2.2 Difference between Single-Machine Job Sequencing Problem and RORO

Most of the time, the dependency relation determines the precedence relation, i.e., if  $r_i^{e_i}$  and  $r_j^{e_j}$  are dependent under  $i < j$ ,  $r_j^{e_j}$  generally cannot be placed ahead of  $r_i^{e_i}$ . For  $r_3^P$  and  $r_7^D$  in Table 3.4, if  $r_7^D$  is placed ahead of  $r_3^P$ , then packet 0100 is evaluated as  $D$ , not  $P$ . Thus,  $r_7^D$  depending on  $r_3^P$  means that  $r_7^D$  is placed behind  $r_3^P$ . However, although  $r_2^P$  and  $r_7^D$  are dependent,  $r_7^D$  can be placed ahead of  $r_2^P$  when  $r_3^P$  is placed ahead of  $r_7^D$ . Only packet 0000 may cause a policy violation with respect to placing  $r_7^D$  ahead of  $r_2^P$ . However, if  $r_3^P$  is placed ahead of  $r_7^D$ , because 0000 is evaluated as  $P$  by  $r_3^P$ , placing  $r_7^D$  ahead of  $r_2^P$  does not cause policy violation. Thus,  $r_j^{e_j}$  depending on  $r_i^{e_i}$  does not always mean that  $r_j^{e_j}$  can not be placed ahead of  $r_i^{e_i}$ .

Avoiding this characteristic of RORO, we can obtain the optimal rule order, if the graph of dependency relations is a forest of oriented trees [34]. That is, by using the algorithm for single-machine job sequencing [34], we can achieve a better ORO solution, if the graph of dependency relations is a forest of oriented trees.

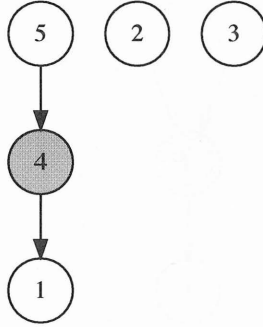


Figure 3.4: Forest of oriented trees.

### 3.3 Rewriting Rules to Oriented Trees

#### 3.3.1 Rewriting Rules

The proposed rule rewriting algorithm begins with an empty rule list  $\mathcal{R}'$ , obtains a rule from the input rule list, and inserts it into  $\mathcal{R}'$  from  $r_1$  to  $r_n$ . If inserting rule  $r_i$  into  $\mathcal{R}'$  does not make the dependency graph of  $\mathcal{R}'$  into a forest of oriented trees, the algorithm expands  $r_i$  into  $r_{i_1}, r_{i_2}, \dots, r_{i_k}$  so that the graph of  $\mathcal{R}' \cup \{r_{i_1}, r_{i_2}, \dots, r_{i_k}\}$  becomes a forest of oriented trees. Note that the algorithm expands  $r_i$  so that at least one rule in  $r_{i_1}, r_{i_2}, \dots, r_{i_k}$  is included in some rule in  $\mathcal{R}'$ . For example, rules  $r_1^P$  to  $r_5^P$  in Table 3.4 form a forest of oriented trees as shown in Fig. 3.4. Adding  $r_6^P$  to the rule list consisting of  $r_1^P$  to  $r_5^P$  violates the property that the dependency graph is a forest of oriented trees as illustrated in Fig. 3.5. The rewriting algorithm expands  $r_6^P$  to  $r_{6_1}^P, r_{6_2}^P$ , and  $r_{6_3}^P$ , as shown in Table 3.5 and inserts  $r_{6_1}^P$  and  $r_{6_2}^P$  into the rule list. Because the set of packets matching  $r_{6_3}^P$  is included in that of  $r_4^P$ , i.e.,  $r_{6_3}^P$  is redundant,  $r_{6_3}^P$  is not inserted into the rule list. The resulting graph of Table 3.5 is shown in Fig. 3.6 as a forest of oriented trees.

#### 3.3.2 Merging Rules

Because expanding a rule consisting of many '\*' generates a lot of rules, the algorithm attempts to remove such rules. If rules  $r_i^e$  and  $r_j^f$  satisfy all of the following conditions, they can be merged:

1. the evaluation types of  $r_i^e$  and  $r_j^f$  are the same,
2.  $r_j^f$  can be placed just behind  $r_i^e$ ,
3. (a)  $r_i^e$  is included in  $r_j^f$  or  $r_j^f$  is included  $r_i^e$ , or  
 (b) the difference in the conditions of  $r_i^e$  and  $r_j^f$  is just one bit.

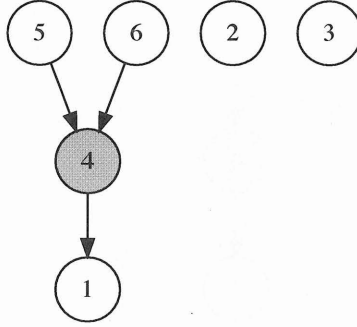


Figure 3.5: Component of 1, 4, 5, and 6 is not an oriented tree.

Table 3.5: Expand  $r_6^P$  to  $r_{6_1}^P$ ,  $r_{6_2}^P$ , and  $r_{6_3}^P$ .

Filter $\mathcal{R}$
$r_4^D = 0 * 1 *$
$r_{6_1}^P = 1 * * 1$
$r_{6_2}^P = 0 * 0 1$
$r_{6_3}^P = 0 * 1 1$

As an example, even if  $r_1^P$  and  $r_2^P$  in Table 3.4 have the same evaluation types, because  $r_1^P$  is not included in  $r_2^P$  and  $r_2^P$  is not included in  $r_1^P$ , and the number of different bits in those rules is 3, they can not be merged. Because the evaluation types of  $r_4^D$  and  $r_6^P$  are different, those rules cannot be merged. Even though  $r_3^P$  is included in  $r_6^P$  and their evaluation types are the same, because  $r_6^P$  can not be placed just behind  $r_3^P$ , those rules cannot be merged. In contrast,  $r_5^P$  and  $r_6^P$  can be merged.

The proposed rule reconstruction algorithm merges redundant rules before rewriting the rules.

### 3.3.3 Experiments

We demonstrate the efficiency of the proposed algorithms by presenting the results of experiments conducted on an Intel Core i7-7820X 3.60 GHz CPU with 131 GB main memory under Cent OS 7.3. We implemented the proposed algorithm, the rule reordering algorithm SGM [77],

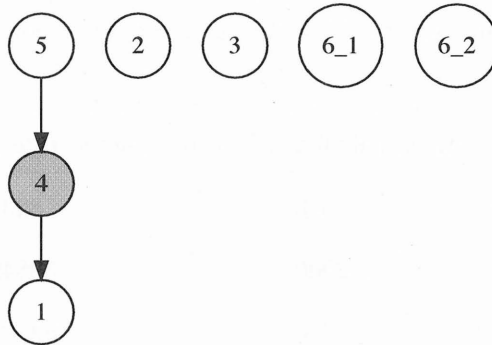


Figure 3.6: Add  $r_{6_1}$  and  $r_{6_2}$ .

the reordering algorithms of Tanaka et al. [75,76] and the latest reordering algorithm of Mohan et al. [61] in C. The rules and headers used in the experiments were generated by the standard packet classification benchmark ClassBench [80]. Because ClassBench generates rules without an action, we added an evaluation type  $P$  or  $D$  to each rule generated by ClassBench with a probability of  $1/2$ . Using ClassBench, we generated standard 5-tuple rules and headers consisting of source/destination addresses, source/destination port numbers and protocol numbers. Because the lengths of these components are 32, 32, 16, 16, and 8 bits respectively, the length of the condition of the rule and header was 104 bits. The number of headers was about 100 times greater than the number of rules.

We measured the latency and the reordering time of a rule list for every algorithm. The medians and the averages of 10 trials for reordering and reconstruction are shown in Figs. 3.7, 3.8, 3.10, and 3.11. Note that we plot the reordering and reconstructing times on a logarithmic scale in Figs. 3.10 and 3.11.

Figure 3.9 shows that the proposed algorithm can increase the latency compared with the given rule list with 1000 and 2000 rules. As shown in Figs. 3.10 and 3.11, the proposed rule reconstruction algorithm is slower than the other rule reordering algorithms. However, Figs. 3.7 and 3.8 show that the proposed rule reconstruction algorithm decreases the median and average latency.

Comparing Figs. 3.7 and 3.8, the median is clearly a better indicator of the proposed algorithm than the average. Table 3.6 suggests that the proposed reconstruction algorithm increases the average number of rules. Indeed, Table 3.7 and Fig. 3.9 show that the proposed algorithm inefficiently increases the number of rules and can, in the worst case, increase the latency. These results indicate that the proposed algorithm is influenced by the characteristics of the given rules. It is important to select the appropriate algorithm for the characteristics of the rule list.

Table 3.6: The average # of rules generated by the proposed algorithm.

given rule list	reconstructed rule list
1000	8236.8
2000	39849.6
3000	53125.4

Table 3.7: The maximum # of rules generated by the proposed algorithm.

given rule list	reconstructed rule list
1000	20811
2000	86548
3000	177906

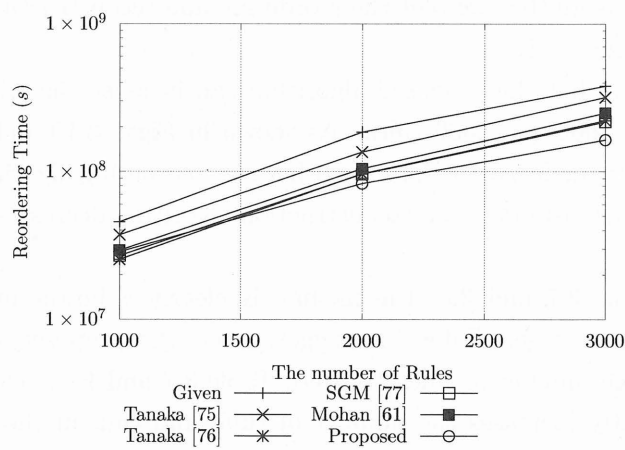


Figure 3.7: Median latency.

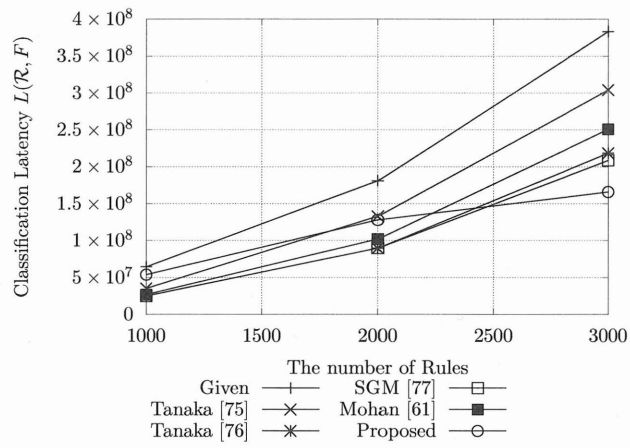


Figure 3.8: Average latency.

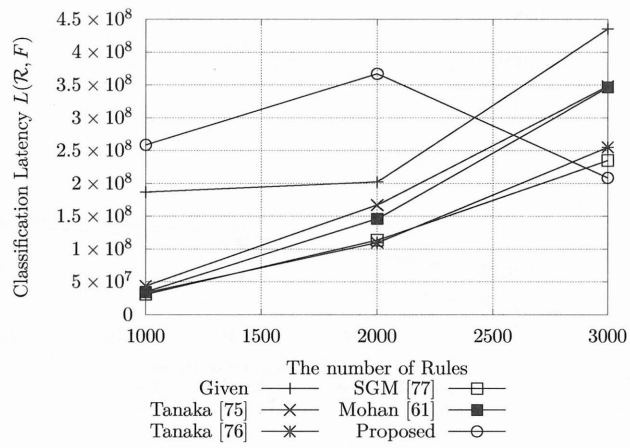


Figure 3.9: Maximum latency.

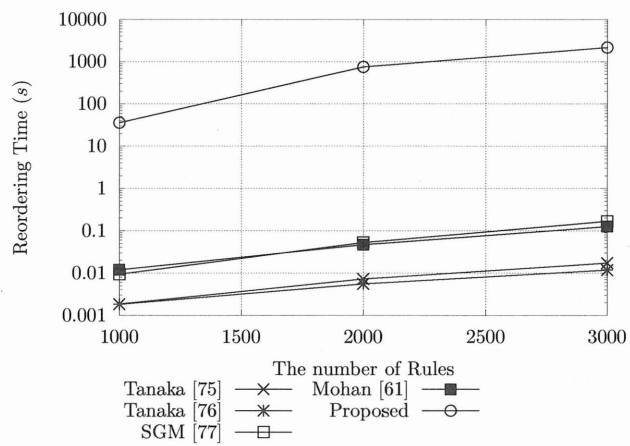


Figure 3.10: Median reordering/reconstructing time.



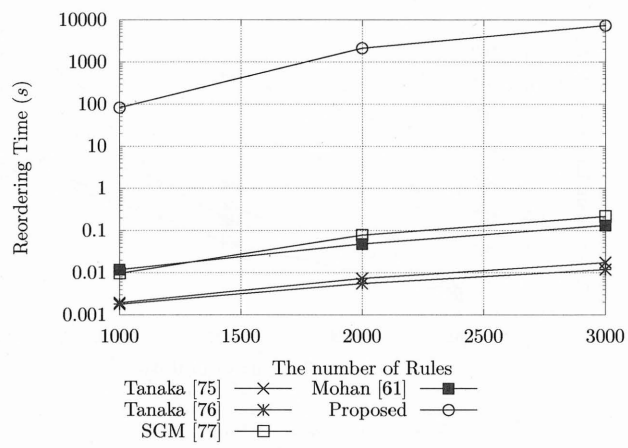


Figure 3.11: Averages of Reordering/Reconstructing Times.

## Chapter 4

# Determining Equivalence of the Rule List Policies

Any algorithm for reordering or reconstructing the rule list must retain its original classification policy. In this chapter, we present an algorithm that determines the equivalence of two rule lists by constructing the ZDD representing these policies. The effectiveness of this algorithm is confirmed through a series of experiments.

Given two decision lists  $L_1$  and  $L_2$ , deciding whether they represent the same Boolean function is **coNP**-complete [23]. Because deciding equivalence of two decision lists can be reduced to deciding equivalence of two rule lists, deciding equivalence of two rule list is also **coNP**-complete.

Therefore, determining the equivalence of reordered or reconstructed rule lists is generally difficult. However, for rule lists of practical size, we can identify policy violations by constructing appropriate ZDDs.

### 4.1 Determining Equivalence of Rule List Policies via ZDD

A procedure for constructing a ZDD according to  $M(r_i)$  is shown in Algorithm 8. Further, a ZDD construction method for  $M(r_i)$  using a BDD/ZDD library such as CUDD [68] is given in Algorithm 9.

Algorithm 8 first constructs ZDD  $Z$  according to the set of the only null combination  $00 \cdots 0$  and sets  $ptr$  to point  $Z$ . By scanning the condition  $r_i^e = b_1 b_2 \cdots b_w$ , it then forms a non-terminal node with numeral  $k$  whose 1 edge points to  $ptr$  and 0 edge points to the 0-terminal node if  $b_k = 1$ , and a non-terminal node with numeral  $k$  in which both edges point to  $ptr$  if  $b_k = *$ , and then  $ptr$  points to a currently generated node. An example of constructing a ZDD using Algorithm 8 is shown in Fig. 4.1.

First, Algorithm 9 constructs ZDD  $Z$  according to the set of the only null combination. Then, by scanning the condition  $r_i^e = b_1 b_2 \cdots b_w$ , it applies the  $\text{change}(k)$  operation to  $Z$  if  $b_k = 1$ , and takes the union of  $Z$  and  $Y$  if  $b_k = *$ , where  $Y$  is  $Z.\text{change}(k)$ . An example of how

---

**Algorithm 8:** make ZDD for Rule  $r$ 

---

**input** : rule  $r_i^e = b_1 b_2 \cdots b_w$   
**output**: ZDD for rule  $r_i^e$

- 1  $i \leftarrow w$  ;
- 2 pointer  $ptr$  to 1-terminal node;
- 3 **while**  $i > 0$  **do**
- 4     **if**  $b_i = '*'$  **then**
- 5         make a non-terminal node  $v$  whose variable is  $i$  and its left and right edges  
       point to  $ptr$  ;
- 6          $ptr$  points to  $v$ ;
- 7     **end**
- 8     **if**  $b_i = '1'$  **then**
- 9         make a non-terminal node  $v$  whose variable is  $i$  and its left edge point to 0 and  
       right edges point to  $ptr$  ;
- 10          $ptr$  points to  $v$ ;
- 11     **end**
- 12      $i \leftarrow i - 1$  ;
- 13 **end**
- 14 **return** ZDD pointed by  $ptr$  ;

---

to construct the ZDD using Algorithm 9 is shown in Fig. 4.2.

Algorithm 10 describes the method of constructing the ZDD according to  $\mathcal{R} = \langle r_1^{e_1}, r_2^{e_2}, \dots, r_n^{e_n} \rangle$ . First, Algorithm 10 constructs the null combination  $Z$  and then scans rules in descending order from  $r_n^{e_n}$ . The method constructs ZDD  $Z_i$  for  $r_i^{e_i}$ . It sets  $Z$  to  $Z \cup Z_i$  if  $e = D$ , or to  $Z \setminus Z_i$  otherwise. An example of constructing the ZDD using Algorithm 10 is shown in Fig. 4.3.

The equivalence of rule lists  $\mathcal{R}_1$  and  $\mathcal{R}_2$  can be confirmed by constructing  $ZDD_1$  and  $ZDD_2$  and checking whether the two ZDDs are the same. The CUDD package and the algorithms presented here implement the ZDD as a hash table and use shared ZDD techniques [59]. Whether two ZDDs,  $A$  and  $B$  are the same depends on whether the addresses of the two ZDDs are the same. Thus, the equivalence of ZDDs can be checked in one step. Thus, we can determine the equivalence of rule lists if the ZDDs for these rule lists can be constructed.

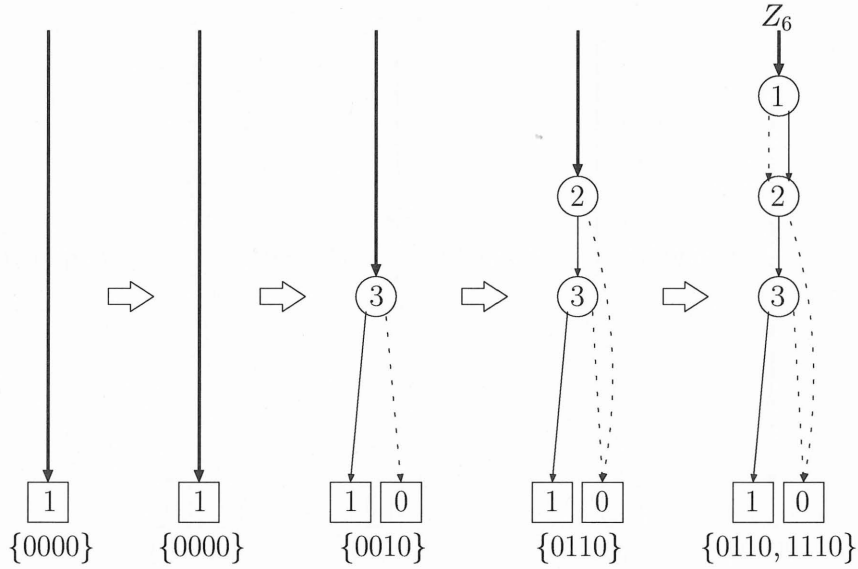


Figure 4.1: Construction process of ZDD according to the set of packets matching  $r_6^D$  by Algorithm 8.

---

**Algorithm 9:** make ZDD for Rule  $r$  using BDD/ZDD Library like CUDD [68]

---

**input** : rule  $r_i^e = b_1 b_2 \dots b_w$   
**output:** ZDD for rule  $r_i^e$

- 1 make ZDD  $Z$  for the set of null combination  $\{00 \dots 0\}$ ;
- 2  $i \leftarrow w$  ;
- 3 **while**  $i > 0$  **do**
- 4 **if**  $b_i = '1'$  **then**  $Z.\text{change}(i)$ ;
- 5 **else if**  $b_i = '*'$  **then**
- 6  $Z \leftarrow Z \cup Z.\text{change}(i)$ ;
- 7 **end**
- 8  $i \leftarrow i - 1$  ;
- 9 **end**
- 10 **return**  $Z$ ;

---

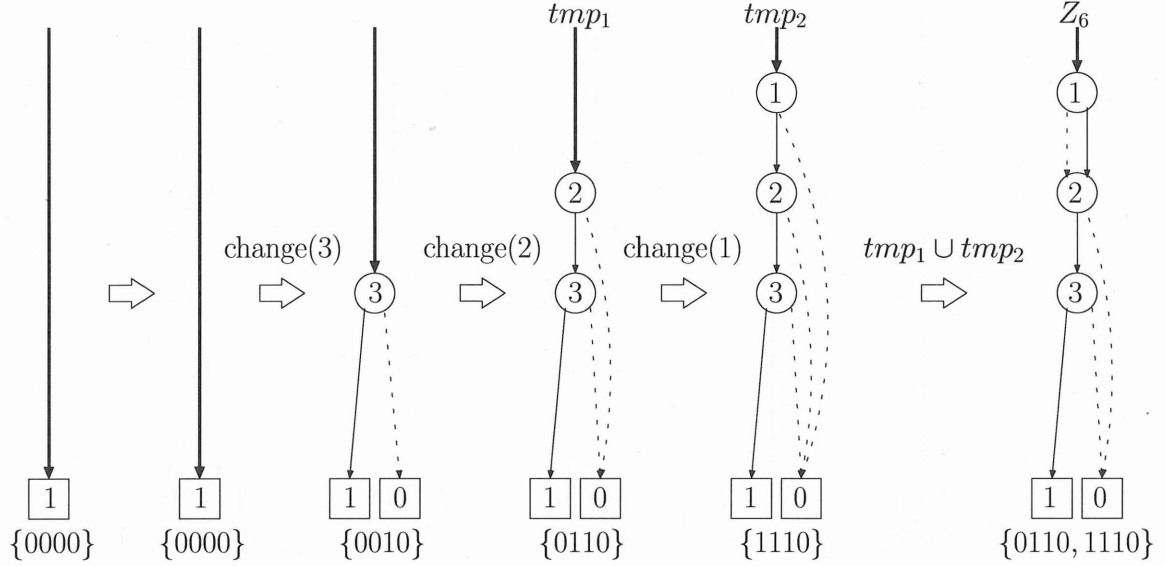


Figure 4.2: Construction process of ZDD according to the set of packets matching  $r_6^D$  by Algorithm 9.

---

**Algorithm 10:** make ZDD for Rule List  $\mathcal{R}$

---

**input** : rule list  $\mathcal{R} = \langle r_1^{e_1}, r_2^{e_2}, \dots, r_n^{e_n} \rangle$

**output:** ZDD for rule list  $\mathcal{R}$

- 1 make zdd  $Z$  for the empty set ;
  - 2  $i \leftarrow n$  ;
  - 3 **while**  $i > 0$  **do**
  - 4     make zdd  $Z_i$  for  $r_i^{e_i}$  by Algorithm 9 ;
  - 5     **if**  $e^i = D$  **then**  $Z \leftarrow Z \cup Z_i$  ;
  - 6     **else**  $Z \leftarrow Z \setminus Z_i$  ;
  - 7      $i \leftarrow i - 1$  ;
  - end**
  - 8 **return**  $Z$  ;
-

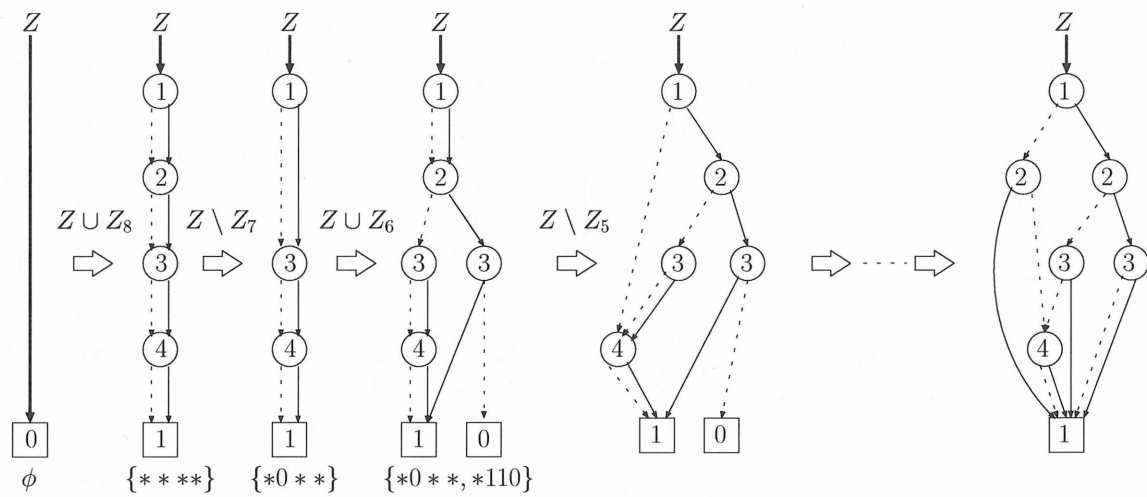


Figure 4.3: Construction process for ZDD via Algorithm 10

Table 4.1: List 1.

Filter $\mathcal{R}_1$
$r_1^B = * 1 1 0$
$r_2^A = 0 * 1 *$
$r_3^B = 1 0 * 0$
$r_4^C = 1 1 0 1$
$r_5^C = 1 1 1 1$
$r_6^D = 1 * * *$
$r_7^A = * 1 * 1$
$r_8^D = * 0 * 0$
$r_9^C = * * * *$

Table 4.2: List 2.

Filter $\mathcal{R}_2$
$r_1^A = 0 0 1 0$
$r_2^B = * * 1 0$
$r_3^C = 0 0 0 1$
$r_4^A = 0 * * 1$
$r_5^D = 1 1 0 0$
$r_6^C = * 1 * *$
$r_7^B = 1 0 0 0$
$r_8^D = 1 0 * 1$
$r_9^D = * * * *$

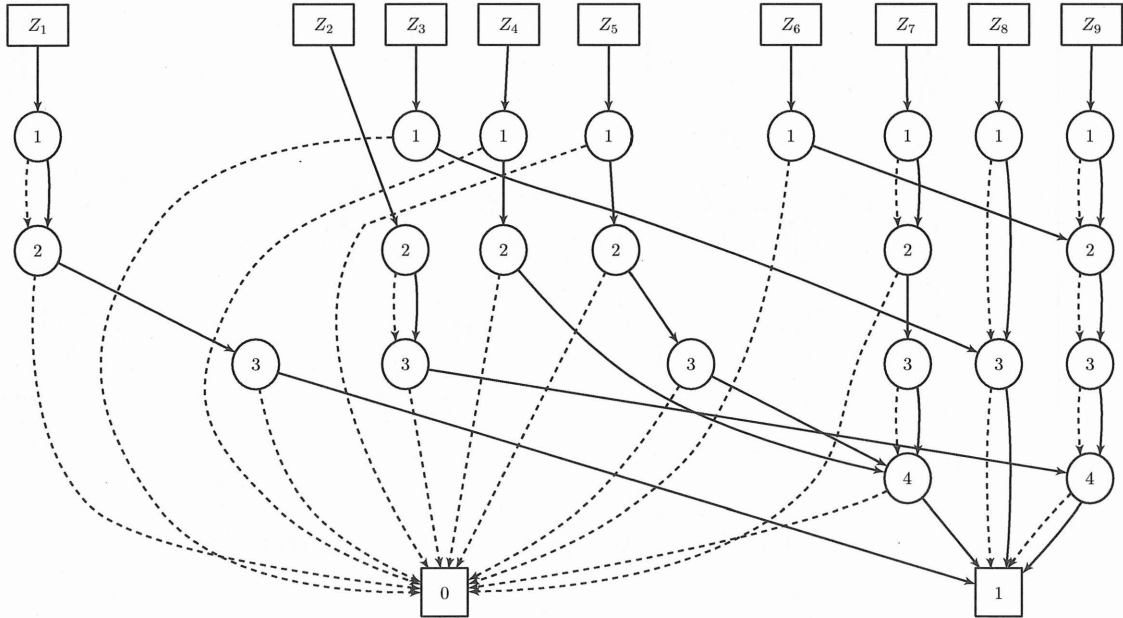


Figure 4.4: ZDDs for rule list in Table 4.1.

## 4.2 Determining Equivalence of Rule Lists with Multiple Actions

In the previous subsection, we presented the algorithms for determining the equivalence of rule lists with only two actions  $P$  and  $D$ . In this section, using Tables 4.1 and 4.2, we introduce an algorithm for determining the equivalence of rule lists that are not limited to two actions. In the following, such a rule list is called a rule list with multiple actions.

To determine the equivalence of rule lists with multiple actions  $A_1, A_2, \dots, A_m$ , the determi-

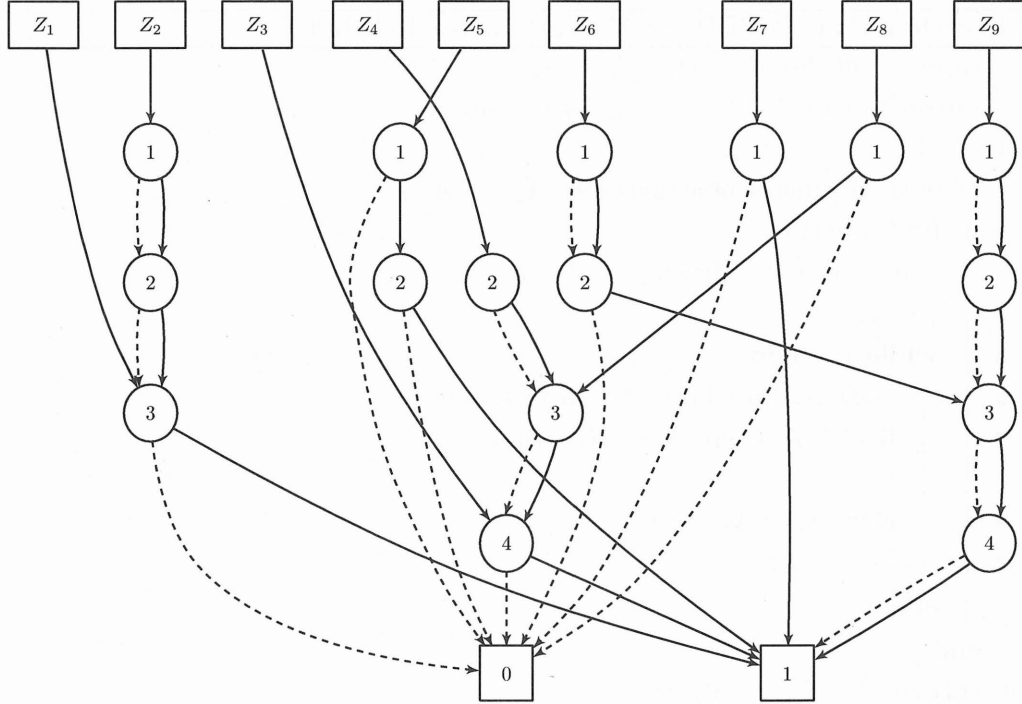


Figure 4.5: ZDDs for rule list in Table 4.2.

Table 4.3: A function  $f : \mathcal{P} \rightarrow \{A, B, C, D\}$  represented by Tables 4.1 and 4.2.

0000 $\mapsto D$	0100 $\mapsto C$	1000 $\mapsto B$	1100 $\mapsto D$
0001 $\mapsto C$	0101 $\mapsto A$	1001 $\mapsto D$	1101 $\mapsto C$
0010 $\mapsto A$	0110 $\mapsto B$	1010 $\mapsto B$	1110 $\mapsto B$
0011 $\mapsto A$	0111 $\mapsto A$	1011 $\mapsto D$	1111 $\mapsto C$

nation method constructs ZDDs as described in the previous section for  $m$  actions.

The procedure for constructing ZDDs  $X_1, X_2, \dots, X_m$  for a rule list with multiple actions is described in Algorithm 11.

Algorithm 11 constructs ZDD  $X_i$  for an action  $A_i$ , repeating the process from line 2 to line 9. The difference between Algorithms 10 and 11 is whether  $A_i$  is specified on line 7.

For rule lists  $\mathcal{R}_1$  and  $\mathcal{R}_2$ , equivalence can be determined by constructing  $2m$  ZDDs  $X_{11}, X_{12}, \dots, X_{1m}$  and  $X_{21}, X_{22}, \dots, X_{2m}$  and checking the equality of ZDDs  $X_{1k}$  and  $X_{2k}$ .

### 4.3 Experiments

To confirm the efficiency of the proposed algorithm for a rule list with only two actions  $P$  and  $D$ , we implemented it in C under the Cent OS Release 6.10 (Final) on an Intel Core i5-3470 3.20 GHz CPU with 2 GB main memory. We generated the rule lists using ClassBench [80] and



---

**Algorithm 11:** make ZDDs for Multiple Actions Rule List  $\mathcal{R}$ 

---

**input** : rule list  $\mathcal{R} = \langle r_1^{e_1}, r_2^{e_2}, \dots, r_n^{e_n} \rangle$   
**output**: ZDDs  $X_1, X_2, \dots, X_m$  for rule list  $\mathcal{R}$

```
1  $i \leftarrow 1$  ;  
  //  $m$  is the number of actions  $\{A_1, A_2, \dots, A_m\}$ ;  
2 while  $i \leq m$  do  
3   make zdd  $X_i$  for the empty set ;  
4    $j \leftarrow n$ ;  
5   while  $j > 0$  do  
6     make zdd  $tmp$  for  $r_j^{e_j}$  by Algorithm 9 ;  
7     if  $e^j = A_i$  then  $X_i \leftarrow X_i \cup tmp$  ;  
8     ;  
9     else  $X_i \leftarrow X_i \setminus tmp$  ;  
10     $i \leftarrow i - 1$  ;  
11  end  
12 end  
13 return  $X_1, X_2, \dots, X_m$  ;
```

---

measured the time for required to determine the equivalence of the rule lists.

Figure 4.7 shows the time required to construct the ZDD by proposed method, where the units of measurement are seconds. Figure 4.7 shows that the time required to determine the equivalence of the rule lists is less than 0.2 s. This shows the remarkable effectiveness of the proposed algorithm. Thus, the proposed method is effective for rule lists of practical size.

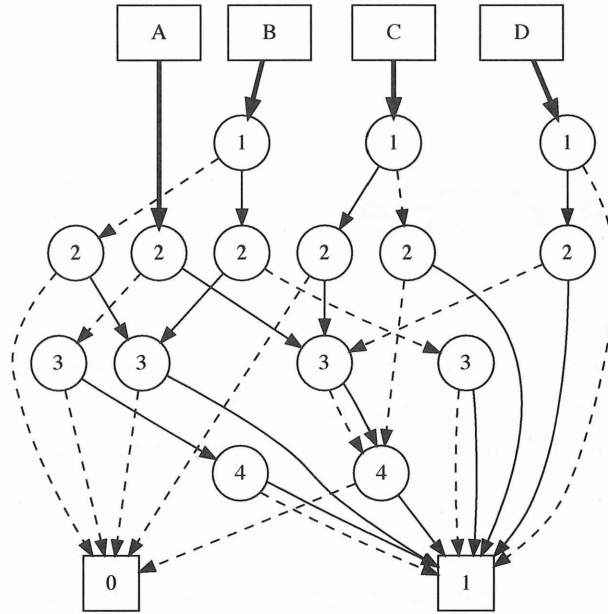


Figure 4.6: ZDDs for policies according to Tables 4.1 and 4.2.

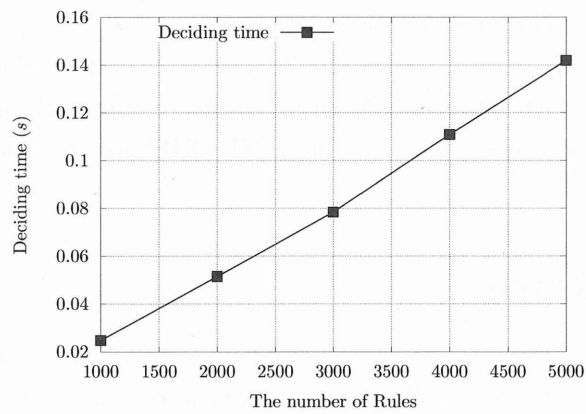


Figure 4.7: Deciding time (s).

## Chapter 5

# Run-Based Trie

In the following section, we will discuss packet classification algorithms.

Mikawa et al. proposed a data structure called a run-based trie (RBT) [57]. They define a run as a bitstring with maximal length and not containing any wild-cards. A run is defined as follows:

**Definition 5.0.1.** (*run form*) Let  $r_i \in \{0, 1, *\}^w$  be a bitmask rule of length  $w$ . A substring  $b_i b_{i+1} \cdots b_j$  ( $1 \leq i \leq j \leq w$ ) of  $r$  that satisfies the following two conditions is called run;

$$i) \quad b_k = 0 \vee b_k = 1 \quad (i \leq k \leq j)$$

$$ii) \quad (i \geq 2 \Rightarrow b_{i-1} = *) \wedge (j \leq w - 1 \Rightarrow b_{j+1} = *).$$

For instance, a bitmask rule of length 16

\* \* 0 1 \* \* 0 0 1 \* \* \* 1 0 1 0

consists of 3 runs, 01, 001, and 1010. These runs begin at the third, 7th, and 13th bits in the rule, respectively. Runs in a rule  $r_i$  are represented as  $\rho_i^1, \rho_i^2, \dots, \rho_i^k$  ( $0 \leq k \leq \lceil w/2 \rceil$ ). An RBT consists of  $w$  tries  $T_1, T_2, \dots, T_w$ . Each trie  $T_k$  is constructed by placing the bit pattern of the run beginning at the  $k$ -th bit of  $r_i \in \mathcal{R}$  on its corresponding path of  $T_k$ . In addition, we mark  $\rho_i^j$  on the path if the run is the  $j$ -th run of  $r_i$ . The RBT for the rule list in Table 5.1 is shown in Fig. 5.1.

### 5.1 Simple Search

A simple RBT search [57] traverses tries  $T_1, T_2, \dots, T_w$  with the bit patterns of the packet beginning at the  $k$ -th bit and collects the runs that match the pattern. The matched rules are then calculated from the collected runs and the highest priority rule in the match rules is returned. If there are no matching rules, the default rule  $r_n$  is returned. For example, packet 01010 traverses the heavy lines in Fig. 5.1 and collects runs  $\rho_1^1, \rho_5^1, \rho_4^1$  and  $\rho_5^2$ . Because 01010 only matches rule  $r_5$ , the highest priority rule for 01010 is  $r_5$ .

Table 5.1: Bitmask rules.

Filter $\mathcal{R}$	
$r_1$	0 * * 0 1
$r_2$	1 * 1 1 *
$r_3$	1 0 0 * *
$r_4$	* 1 0 * 1
$r_5$	0 * * 1 *
$r_6$	* * * * *

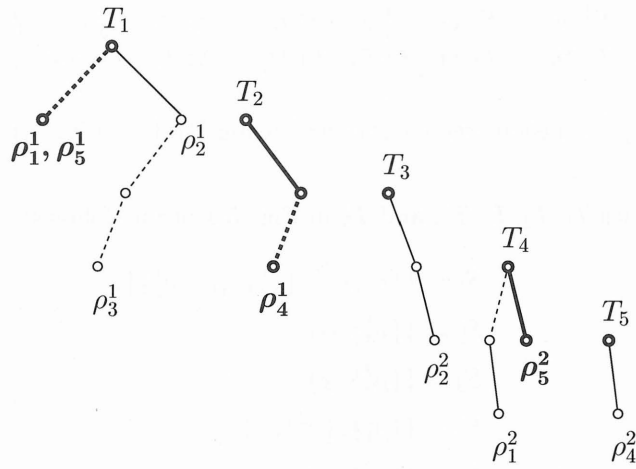


Figure 5.1: Run-based trie for rule list in Table 5.1.

Let us compute the time complexity of this simple search. First, to traverse tries  $T_1, T_2, \dots, T_k$ , the simple search requires  $w + (w - 1) + \dots + 1$  steps. The time complexity of traversing all tries is  $O(w^2)$ . Then, because the number of runs on the tries is at most  $n \times \lceil w \rceil$ , the time complexity required for comparing the runs is  $O(nw)$ . Thus, the time complexity of the simple search is  $O(nw + w^2)$ .

## 5.2 Decision Tree constructed from RBT

Mikawa et al. also proposed a search algorithm using a decision tree constructed from an RBT [57]. Because there is a limited number of patterns used to collect runs for each trie  $T_i$  in an RBT search, the patterns are enumerated as  $S_1, S_2, \dots, S_w$ . For instance, the patterns used

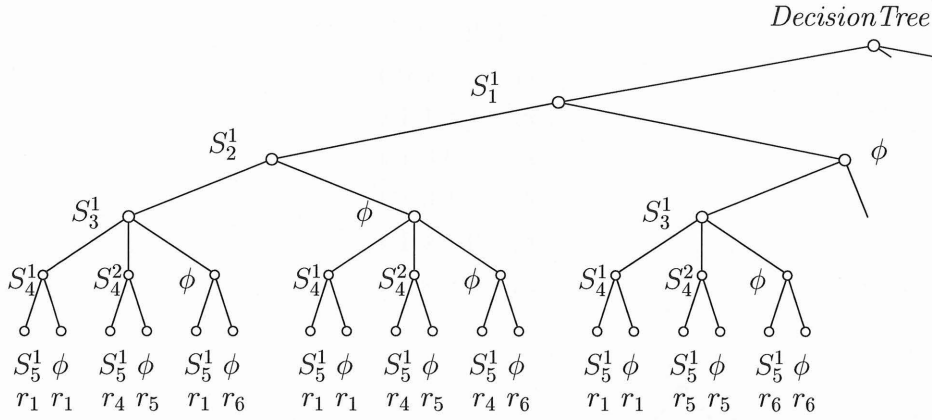


Figure 5.2: Decision tree constructed using RBT in Fig. 5.1 (rewritten).

to collect runs for tries  $T_1, T_2, T_3, T_4$ , and  $T_5$  in Fig. 5.1 are as follows:

$$\begin{aligned}
 S_1 &= \{\{\rho_1^1, \rho_5^1\}, \{\rho_2^1\}, \{\rho_2^1, \rho_3^1\}\}, \\
 S_2 &= \{\{\rho_4^1\}, \phi\}, \\
 S_3 &= \{\{\rho_2^2\}, \phi\}, \\
 S_4 &= \{\{\rho_1^2\}, \{\rho_5^2\}, \phi\}, \\
 S_5 &= \{\{\rho_4^2\}, \phi\},
 \end{aligned} \tag{5.1}$$

where  $\phi$  denotes no match with a run.

Based on these patterns, the decision tree is constructed by taking the Cartesian product of  $S_1 \times S_2 \times \dots \times S_w$ . The decision tree constructed from the patterns in Eq. 5.1 is shown in Fig. 5.2. Each path from the root to a leaf of the decision tree is equivalent to a search path obtained by traversing the RBT from  $T_1$  to  $T_w$ . Computing the highest-priority rule for each path on the decision tree in advance, we obtain the highest priority rule by only traversing the decision tree using the RBT. The time complexity of this decision tree search is  $O(w^2)$ , because we can reach a leaf by traversing the RBT.

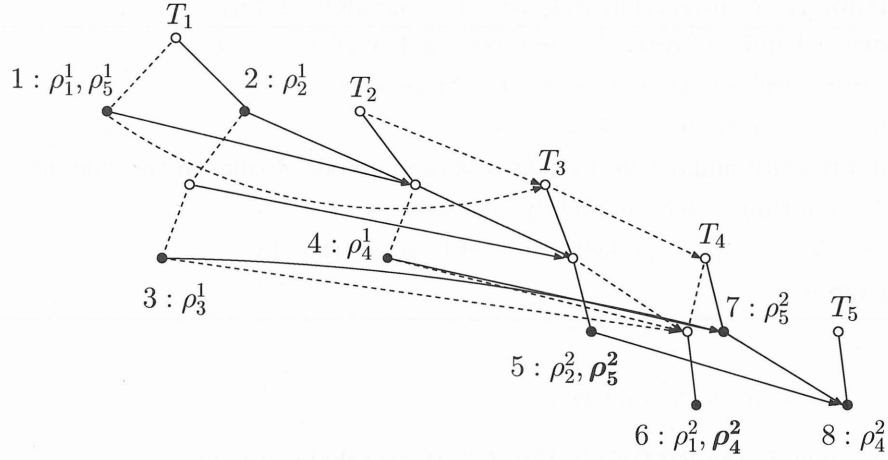


Figure 5.3: RBTwP for rule list in Table 5.1.

## 5.3 Decision Tree based on RBT with Pointers

### 5.3.1 RBT with Pointers

In the worst case, the RBT search accesses the bitstring of a packet  $w^2$  times. Even if it reaches down to a node at depth  $k$  on  $T_k$ , the next starting point is the root of  $T_{k+1}$ . Because searching for runs at nodes of depth  $k$  means that bits  $p[1]$  to  $p[k+d-1]$  have already been referenced, traversing from the root of  $T_{k+1}$  to a node at depth  $k$  is redundant. Focusing on this point, we propose a search method that refers to the bits of a packet at most  $w$  times. This method adds new arcs to a non-terminal node that has no 0-arc or 1-arc. In addition, a run from a node on  $T_k$  is copied to nodes on  $T_1, \dots, T_{k-1}$ . For the rule list in Table 5.2, an RBT with added arcs and copied runs is shown in Fig. 5.3. We call this an RBT with pointers (RBTwP). Traversing the RBTwP, we access the bitstring of a packet at most  $w$  times, in searching for the highest-priority rule for the packet. Thus, the time complexity and space complexity of this method are  $O(w)$  and  $O(nw)$ , respectively.

### 5.3.2 Decision Tree based on RBTwP

As well as the decision tree constructed from naive RBT [57], we can construct a decision tree based on RBTwP.

First, we number the nodes that have run (denoted by the numeral on the left side of the colon in Fig. 5.3). We call this number the *node number*. The set of reachable node numbers from node  $i$  is limited according to Eq. 5.1. This reachable set is defined as follows:

**Definition 5.3.1.** (*Reachable set in RBTwP*)

$$N_i = \{ k \mid \text{there exists a path } p \text{ from } i \text{ to } k, \neg \exists j \in p \}, \quad (5.2)$$

---

**Algorithm 12:** ConstructionOfDecisionTreeBaesdOnRBTwP

---

**input** : Family of reachable sets  $root$  and  $N_1, N_2, \dots, N_k$

**output**: Decision Tree based RBT with pointers

- 1 make a root node of decision tree  $d$  ;
  - 2 add a priority number  $[n]$  to  $d$  //  $n$  is the number of rules in the rule list;
  - 3 call Algorithm 13 with explicitly  $root$  and  $d$ ;  
//  $N_1, N_2, \dots, N_k$  is implicitly passed to Algorithm 13 ;
  - 4 return  $d$  ;
- 

where  $i, j$ , and  $k$  are node numbers.

For example, in the RBTwP in Fig. 5.3, the reachable sets are

$$\begin{aligned} root &= \{1, 2\}, \\ N_1 &= \{4, 5, 6, 7\}, \\ N_2 &= \{3, 4, 5, 6\}, \\ N_3 &= \{6, 7\}, \\ N_4 &= \{6, 7\}, \\ N_5 &= \{8\}, \\ N_6 &= \phi, \\ N_7 &= \{8\}, \\ N_8 &= \phi, \end{aligned} \tag{5.3}$$

where  $root$  is the root node of  $T_1$ .

Based on these sets, we construct the decision tree using the Cartesian product-like operation shown in Algorithm 12. Algorithm 12 forms a decision tree by calling Algorithm 13, in which lines 1–5 recursively make node  $i$  based on  $N_i$  and calculate the highest-priority rule at node  $i$ .

Because this decision tree can be searched by the RBTwP at most  $w$  steps, the time complexity of this decision tree search is  $O(w)$ .

Although this decision tree is very efficient in terms of search time complexity, it may have redundant sub-trees. As shown in Fig. 5.5, the sub-trees in the shaded area are redundant, because a node on the sub-tree has no priority rule  $[i]$  greater than the highest rule on preceding nodes. Thus, such a sub-tree can be pruned.

---

**Algorithm 13: SpanEdges**


---

**input** : Reachable Set  $N$  and a node of decision tree  $v$   
**1** **foreach**  $i \in N$  **do**  
**2**     make a decision tree node  $i$  and an edge from  $v$  to  $i$  ;  
**3**     calculate the candidate highest priority rule number  $c$  ;  
**4**     **if**  $c$  is less than the priority rule of ancient node **then**  
**5**         | add  $[c]$  to  $i$  ;  
**6**     **end**  
**7**     call Algorithm 13 with  $N_i$  and  $i$  ;  
**8** **end**

---

Decision Tree constructed on RBT with pointers

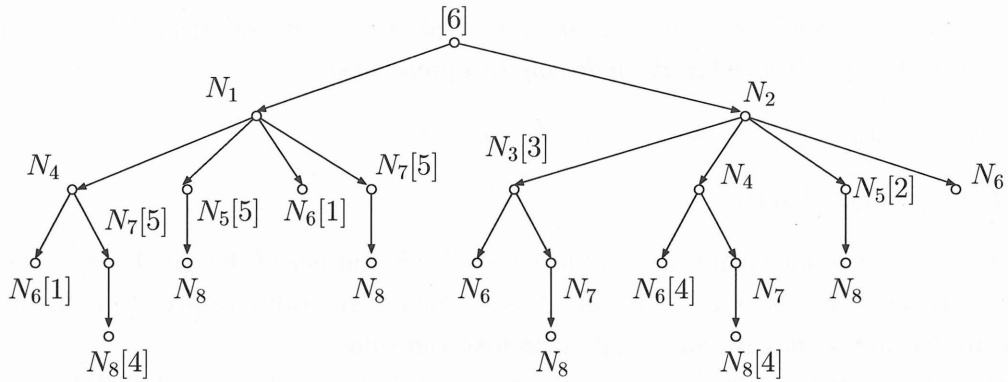


Figure 5.4: Decision tree constructed on RBTwP in Fig. 5.3.

Decision Tree constructed on RBT with pointers

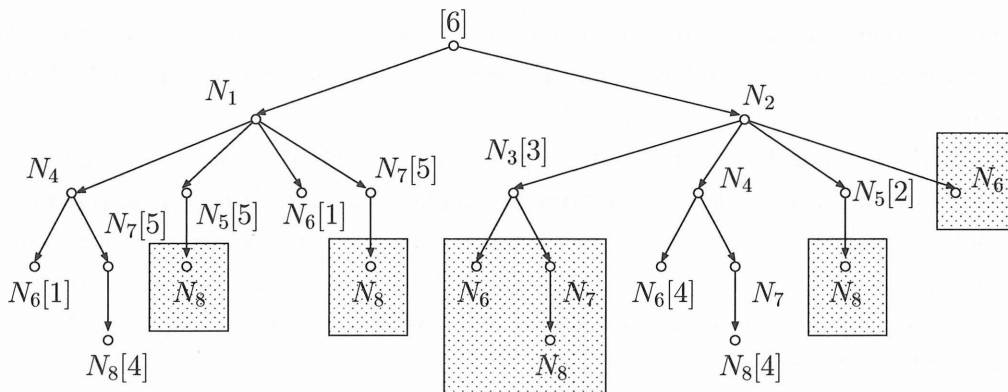


Figure 5.5: Redundant sub-tree in decision tree constructed on RBTwP



## 5.4 Cascaded Circular-RBT

The time complexity of an RBT search depends on  $n$  as  $O(nw + w^2)$ , because there are at most  $n\lceil w/2 \rceil$  runs on the RBT, and a comparison occurs when there is a run on a node when traversing the RBT. If each rule in a rule list has just one run, we can classify a packet in constant time, i.e., independent of the number of rules, via a modified RBT. In this section, we first propose a data structure for the rule list consisting of circular-run rules. Secondly, we provide definitions for the consecutive ones property (C1P) [9] and the circular ones property (Circ1P) [17, 81]. We then propose a packet classification algorithm called cascaded circular-RBT.

### 5.4.1 Circular-RBT

We define a circular-run as follows:

**Definition 5.4.1.** (*circular-run*) Let  $r_i \in \{0, 1, *\}^w$  be a bitmask rule of length  $w$ . A substring of  $r$  is called *circular-run* if it consists of a single run or its substring  $b_i b_{(i+1)} \cdots b_w b_1 \cdots b_j$  ( $1 \leq i \leq w, 1 \leq j < i$ ) satisfies the following two properties:

$$i) \quad b_k = 0 \vee b_k = 1 \quad (i \leq k \leq w \vee 1 \leq k \leq j)$$

$$ii) \quad b_l = * \quad (j < l < i).$$

As an example, for  $r_2$  and  $r_3$  in Table 5.2, each rule consists of the circular-run 111 and 001. These circular-runs begin at the fifth and fourth bits in the rules, respectively. In this section, we consider only a rule list consisting of circular-run rules.

Because a rule has just one run, the superscript  $j$  of a mark  $\rho_i^j$  on the RBT is redundant. Thus, we denote a run in a circular-run rule by  $\rho_i$  instead of  $\rho_i^j$ . When a node on the RBT has more than one run, because all except the run of the highest priority rule are redundant, those redundant runs are removed. Because every rule has just one run, if a packet matches run  $\rho_i$ , then the packet also matches rule  $r_i$ .

For an RBT constructed from a rule list consisting of circular-run rules, if node  $v$  has run  $\rho_i$  and no node that can be reached from a  $b$ -arc of  $v$  has a higher-priority run than  $\rho_i$ , we remove the  $b$ -arc of  $v$ , where  $b$  is 0 or 1. Figure 5.8 shows the circular-RBT (CircRBT) formed by removing redundant arcs from Fig. 5.7.

Although circular-RBT can classify a packet in constant time, i.e., independent of  $n$ , they can only be applied to a rule list consisting of circular-run rules. However, in general, a rule list consists of non-circular-run rules. Thus, we regard a rule list as a binary matrix and permute it such that the matrix has Circ1P [17, 81]. In the following, we say that a rule list has Circ1P if the binary matrix reduced from the rule list has Circ1P. If a rule list has Circ1P, we can apply the CircRBT method to the rule list.

Table 5.2: Circular-run rules.

Filter $\mathcal{R}$	
$r_1$	0 0 1 * *
$r_2$	1 1 * * 1
$r_3$	1 * * 0 0
$r_4$	* * 1 1 0
$r_5$	0 1 * * *
$r_6$	* * * * *

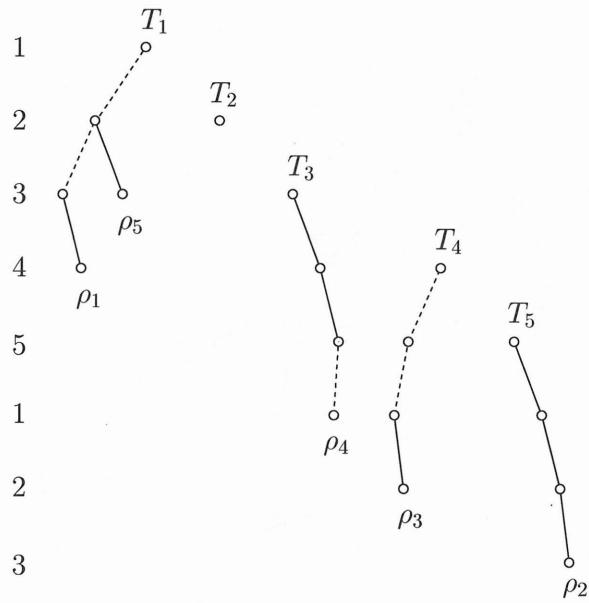


Figure 5.6: RBT for rule list in Table 5.2.

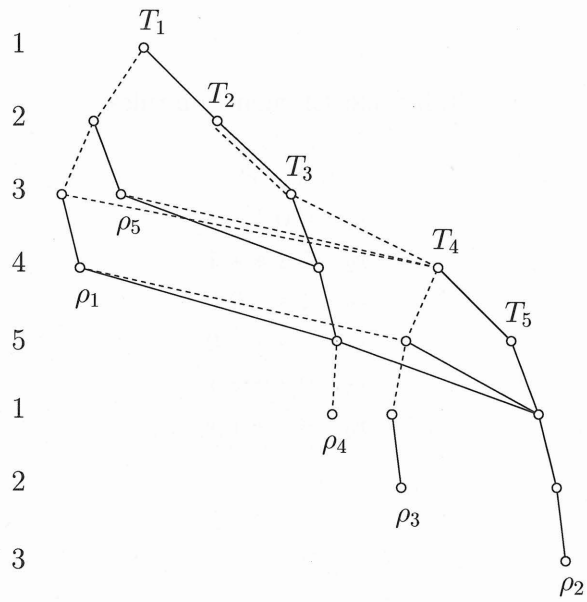


Figure 5.7: RBT added arcs and copied runs for rule list in Table 5.2.

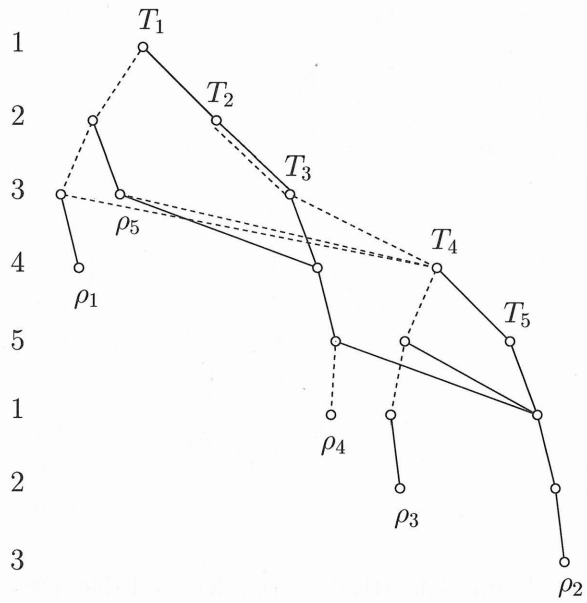


Figure 5.8: Circular-RBT for rule list in Table 5.2.

Table 5.3: Bitmask rules (rewritten).

	Filter $\mathcal{R}$
$r_1$	0 * * 0 1
$r_2$	1 * 1 1 *
$r_3$	1 0 0 * *
$r_4$	* 1 0 * 1
$r_5$	0 * * 1 *
$r_6$	* * * * *

Table 5.4: Replacing 0, 1 by 1 and \* by 0.

	$c_1$	$c_2$	$c_3$	$c_4$	$c_5$
	1	0	0	1	1
	1	0	1	1	0
	1	1	1	0	0
	0	1	1	0	1
	1	0	0	1	0
	0	0	0	0	0

### 5.4.2 Consecutive Ones Property and Circular Ones Property

Replacing the 1s and 0s in a rule by 1 and the \* in the rule by 0, we reduce the problem of whether a rule list has Circ1P to whether a binary matrix has Circ1P. For example, whether the rule list in Table 5.3 has Circ1P can be determined by reducing it to the binary matrix in Table 5.4 and checking whether the matrix has C1P. To explain the Circ1P, we first define C1P.

**Definition 5.4.2.** (*Consecutive ones property (C1P)*) A binary matrix has C1P if there is a permutation of its columns such that the 1s are consecutive in each row. A binary matrix that has C1P is called a C1P matrix and a binary matrix that does not have C1P is called a non-C1P matrix.

For instance, the binary matrix in Table 5.5 has C1P, because there is a permutation  $1 \rightarrow 1$ ,  $2 \rightarrow 3$ ,  $3 \rightarrow 2$  and  $4 \rightarrow 4$  such that the 1s in each row in the permuted matrix are consecutive (see Table 5.6). In contrast to the binary matrix in Table 5.5, that in Table 5.7 is non-C1P.

Using partition refinement [27, 90], the problem of whether an  $n \times r$  binary matrix has C1P is solvable in  $O(n + r + c)$  steps, where  $c$  is the number of 1s in  $M$ .

**Definition 5.4.3.** (*Circular ones property (Circ1P)*) A binary matrix has Circ1P if there is a permutation of its columns such that the 1s or 0s are consecutive in each row. A binary matrix that has Circ1P is called a Circ1P matrix, and a binary matrix that does not have Circ1P is called a non-Circ1P matrix.

Suppose a binary matrix is wrapped around a vertical cylinder. If the columns can be permuted such that the 1s in each row are consecutive on the cylinder, then the matrix has Circ1P. The binary matrix in Table 5.8 has Circ1P, because it can be permuted so that the 0s are consecutive for each row (see Table 5.9). In contrast, the matrix in Table 5.10 is non-Circ1P.

Whether a binary matrix has Circ1P can be determined by complementing those rows whose first column is 1 (i.e., row  $M_1, M_2, \dots, M_r$  is complemented if  $M_{i1} = '1'$ ) and checking whether the matrix has C1P [81]. As we can determine whether a matrix has C1P in  $O(n + r + c)$  steps, Circ1P can be checked in  $O(nr)$  steps.

Table 5.5: C1P-matrix.

$c_1$	$c_2$	$c_3$	$c_4$
1	0	1	0
1	1	1	1
0	1	1	0
0	1	0	1
1	0	1	0
0	0	1	0

Table 5.6: Rearranging columns.

$c_1$	$c_3$	$c_2$	$c_4$
1	1	0	0
1	1	1	1
0	1	1	0
0	0	1	1
1	1	0	0
0	1	0	0

Table 5.7: Non-C1P matrix.

$c_1$	$c_2$	$c_3$	$c_4$
1	1	0	0
1	1	1	1
0	1	1	1
0	0	1	1
0	1	1	0
0	1	0	1

Table 5.8: Circ1P-matrix.

$c_1$	$c_2$	$c_3$	$c_4$	$c_5$
1	0	1	0	1
1	1	0	1	0
0	0	0	1	1
1	1	1	0	1
0	0	0	1	0
0	0	1	0	1

Table 5.9: Rearranging columns.

$c_5$	$c_3$	$c_1$	$c_2$	$c_4$
1	1	1	0	0
0	0	1	1	1
1	0	0	0	1
1	1	1	1	0
0	0	0	0	1
1	1	0	0	0

Table 5.10: Non-Circ1P matrix.

$c_1$	$c_2$	$c_3$	$c_4$	$c_5$
1	0	1	0	1
1	1	0	0	0
0	1	1	0	0
0	1	1	1	0
1	1	1	1	0
0	1	0	0	1

### 5.4.3 Cascaded Circular-RBT

Although the CircRBT method is efficient with respect to both time and space, it can only be applied to a rule list that has Circ1P. In general, because a rule list is non-Circ1P, CircRBT cannot be applied. In this section, we propose an algorithm that divides a rule list into multiple rule lists that have Circ1P, then constructs CircRBTs for these rule lists. Finally, a list of CircRBTs is constructed and used to classify packets.

We present a method of partitioning a rule list in Algorithm 14. First, this algorithm makes a rule list  $\mathcal{R}_1$  consisting of  $r_1$  and  $r_2$ . Then, it repeats the process of taking one of the remaining rules and inserting it into the existing rule list or creating new rule list in order from  $r_3$  to  $r_n$ .

When rule list  $\mathcal{R}$  has fewer than 3 rules, the algorithm returns the only  $\mathcal{R}$ , because the rule list must have Circ1P. If rule list  $\mathcal{R}$  has more than 2 rules, rule list  $S$  (consisting of the head and second element of  $\mathcal{R}$ ) is inserted into  $L_{\mathcal{R}}$  on lines 4–7. Lines 8–19 search for a rule list  $\mathcal{R}$  such that  $\{r\} \cup \mathcal{R}_i$  has Circ1P, and insert  $r$  into  $\mathcal{R}_i$  if there is such a rule list; otherwise, a new rule list  $S$  consisting of only  $r$  is created and inserted into  $\mathcal{R}$ . For instance, given the rule list in Table 5.11, Algorithm 14 divides it into the three rule lists in Tables 5.12, 5.13, and 5.14.

For a series of rule lists having Circ1P,  $L_{\mathcal{R}} = [\mathcal{R}_1, \mathcal{R}_2, \dots, \mathcal{R}_k]$ , we construct a list of CircRBTs  $L_{\mathcal{F}} = [\mathcal{F}_1, \mathcal{F}_2, \dots, \mathcal{F}_k]$ . We call this a cascaded CircRBT. A method of packet classification using cascaded CircRBT is shown in Algorithm 15. This algorithm applies a circular-run-

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**Algorithm 14: RuleListPartition**

---

```
input : Rule list  $\mathcal{R}$ 
output: List of rule list  $L_{\mathcal{R}} = [\mathcal{R}_1, \mathcal{R}_2, \dots, \mathcal{R}_k]$ 
1 make an empty list of rule list  $L_{\mathcal{R}}$  ;
  if  $|\mathcal{R}| < 3$  then
2   | add  $\mathcal{R}$  to  $L_{\mathcal{R}}$  ;
3   | return  $L_{\mathcal{R}}$  ;
  end
4 make a new rule list  $S$  ;
5 add  $\text{head}(\mathcal{R})$  to  $S$  and remove  $\text{head}(\mathcal{R})$  ;
6 add  $\text{head}(\mathcal{R})$  to  $S$  and remove  $\text{head}(\mathcal{R})$  ;
7 add  $S$  to  $L_{\mathcal{R}}$  ;
8 while  $\mathcal{R} \neq \emptyset$  do
9   |  $r \leftarrow \text{head}(\mathcal{R})$  ;
10  |  $it \leftarrow \text{head}(L_{\mathcal{R}})$  ;
11  |  $flag = \text{false}$  ;
12  | while  $it \neq L_{\mathcal{R}}.\text{end}$  do
13  |   | if  $*it \cup \{r\}$  has Circ1P then
14  |   |   | add  $r$  to  $*it$  ;
15  |   |   |  $flag = \text{true}$  ;
16  |   |   | break ;
17  |   |   | end
18  |   |  $it \leftarrow it.\text{next}$  ;
19  |   | end
20  |   | if  $flag \neq \text{true}$  then
21  |   |   | make a new rule list  $S$  ;
22  |   |   | add  $r$  to  $S$  ;
23  |   |   | add  $S$  to  $L_{\mathcal{R}}$  ;
24  |   |   | end
25  |   | remove  $r$  from  $\mathcal{R}$  ;
26  |   | end
27  | end
28 end
```

---

based search to a packet in the order  $\mathcal{F}_1$  to  $\mathcal{F}_k$ , and returns the highest-priority rule number from those obtained from circular-run-based searches. On line 3,  $\mathcal{F}_i(p)$  returns a rule number obtained by searching CircRBT  $\mathcal{F}_i$  with  $p$ . The time and space complexity of this packet classification algorithm are  $O(kw)$  and  $O(nw)$ , respectively, where  $k$  is the size of the list of CircRBT. If  $k$  is independent of  $n$ , we have a constant time packet classification that is independent of the number of rules.

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**Algorithm 15:** ListOfCircRBTSearch
 

---

**input** : List of CircRBT  $L_{\mathcal{F}}$  and packet  $p$   
**output**: Highest priority rule number for  $p$   
 1  $cand \leftarrow n + 1$  //  $n$  is the number of rules ;  
 2  $i \leftarrow 0$  ;  
 while  $i < |L_{\mathcal{F}}|$  do  
 3      $c \leftarrow \mathcal{F}_i(p)$  ;  
    **if**  $c < cand$  **then**  
 4     |  $cand \leftarrow c$  ;  
    **end**  
 5      $i \leftarrow i + 1$  ;  
**end**  
 6 **return**  $cand$  ;

---

Table 5.11: Example of non-Circ1P rule list.

	$c_1$	$c_2$	$c_3$	$c_4$	$c_5$	$c_6$	$c_7$	$c_8$	$c_9$	$c_{10}$	$c_{11}$	$c_{12}$
$r_1$	1	*	0	*	1	1	0	*	*	*	0	1
$r_2$	1	0	*	0	*	1	0	0	0	*	1	*
$r_3$	0	1	0	1	0	1	*	*	0	0	*	*
$r_4$	*	1	0	*	1	0	*	1	0	1	*	1
$r_5$	*	0	1	1	*	*	*	*	*	1	*	*
$r_6$	1	0	0	0	*	*	*	*	1	*	*	0
$r_7$	*	1	*	*	1	0	0	*	*	*	0	0
$r_8$	0	*	1	0	0	0	*	0	*	0	*	*
$r_9$	*	*	*	*	*	*	*	*	*	*	*	*

#### 5.4.4 Experiments

We demonstrate the efficiency of the proposed algorithm through a series of experiments and comparisons with a linear search, Grouper [50], and MDD [71]. An open-source implementation is available for Grouper, whereas the linear search, a classification algorithm using MDD, and the proposed algorithm were implemented in C. Experiments were conducted under the Cent

Table 5.12: Circ1P rule list 1.

	$c_{12}$	$c_5$	$c_3$	$c_{10}$	$c_2$	$c_8$	$c_9$	$c_4$	$c_1$	$c_7$	$c_{11}$	$c_6$
$r_1$	1	1	0	*	*	*	*	*	1	0	0	1
$r_2$	*	*	*	*	0	0	0	0	1	0	1	1
$r_4$	1	1	0	1	1	1	0	*	*	*	*	0
$r_9$	*	*	*	*	*	*	*	*	*	*	*	*

Table 5.13: Circ1P rule list 2.

	$c_{12}$	$c_9$	$c_1$	$c_4$	$c_3$	$c_2$	$c_{10}$	$c_5$	$c_6$	$c_7$	$c_8$	$c_{11}$
$r_3$	*	0	0	1	0	1	0	0	1	*	*	*
$r_5$	*	*	*	1	1	0	1	*	*	*	*	*
$r_6$	0	1	1	0	0	0	*	*	*	*	*	*

Table 5.14: Circ1P rule list 3.

	$c_{10}$	$c_8$	$c_4$	$c_3$	$c_1$	$c_6$	$c_5$	$c_2$	$c_7$	$c_{11}$	$c_{12}$	$c_9$
$r_7$	*	*	*	*	*	0	1	1	0	0	0	*
$r_8$	0	0	0	1	0	0	0	*	*	*	*	*

OS Release 6.8 (Final) on an Intel Core i5-3470 3.20 GHz CPU with 2 GB main memory. We generated the rules and the headers based on the standard benchmark for packet classification algorithms, ClassBench [80]. ClassBench provides `acl`, `fw`, and `ipc` seed files. To generate the rule for these experiments, the `ipc` seed file was used. The original rules generated by ClassBench were converted to arbitrary bitmask rules. The original rules consisted of five fields, namely the source/destination address, source/destination port number, and protocol number. Because these fields have lengths of 32, 32, 16, 16, and 8 bits, respectively, the length of the rule and header was 104 bits. The number of headers was about  $1M$ .

Using the generated rules and headers, we measured the time and memory requirements of constructing the data structures and the time required to determine the highest-priority rule for every algorithm. The construction and search processes were measured in seconds.

Table 5.15 presents the number of instances for which MDD and the proposed data structure could not be constructed within 4 h. As can be seen from Table 5.15 and Figs 5.9 and 5.11, MDD and the proposed algorithm are relatively slow and consume significant amounts of memory.

The means of 10 trials (except instances exceeding 4 h) are shown in Figs. 5.9, 5.10, and 5.11. Note that the time and memory are plotted on a logarithmic scale in Figs. 5.9 and 5.11. As MDD cannot be constructed within 4 h when there are 5000 rules, we do not show these results in Figs. 5.9, 5.10, and 5.11.

The proposed partitioning algorithm makes multiple calls to a routine that determines whether the rule list has Circ1P, and this routine requires the construction of a new graph for the rule list, wasting information that might have been collected from previous calls. Thus, as shown in Fig. 5.9, the proposed algorithm might take a significant amount of time to construct cascaded CircRBT.

In the experiments, Grouper required the least memory to make the lookup table. Thus, although the space complexity of the proposed algorithm is theoretically better than that of Grouper  $2^w/t \cdot tn$  and  $O(nw)$ , the memory requirements of Grouper are lower than those of the proposed algorithm.

Figure 5.10 shows that the search times for the linear search and Grouper [50] are dependent on the number of rules. Although MDD can classify packets in constant time up to 3000 rules, it



Table 5.15: # of instances exceeding 4 h construction time in ipc.

	1000	2000	3000	4000	5000
Grouper	0	0	0	0	0
MDD	0	1	4	2	10
Proposed Algorithm	0	1	0	1	2

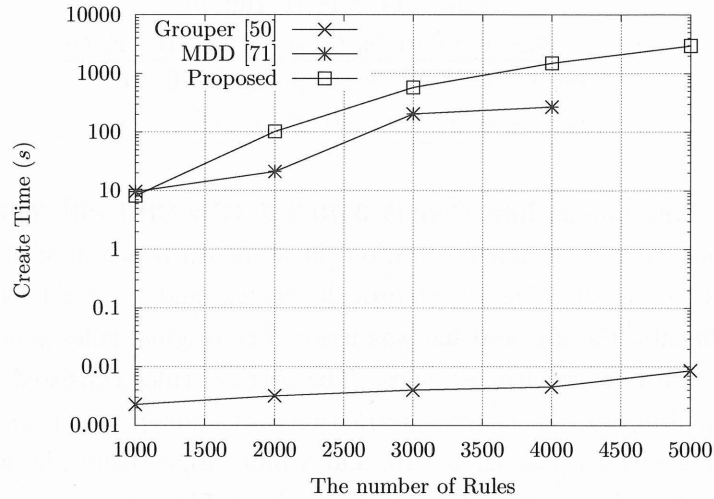


Figure 5.9: Construction times (s).

takes significantly more time for more than 4000 rules. As MDD exceeds the 2GB main memory with 4000 rules, it takes much more time to classify packets. In contrast, the proposed algorithm classifies packets in constant time, independent of the number of rules. This agrees with the theoretical performance in Table 1.8. Because the rules generated by ClassBench are easy to partition, the size of the list of CircRBT list is small, allowing the proposed algorithm to classify packets in a constant time that is independent of the number of rules.

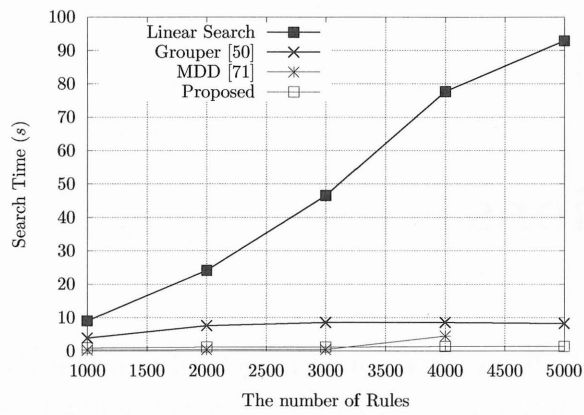


Figure 5.10: Classification times (s).

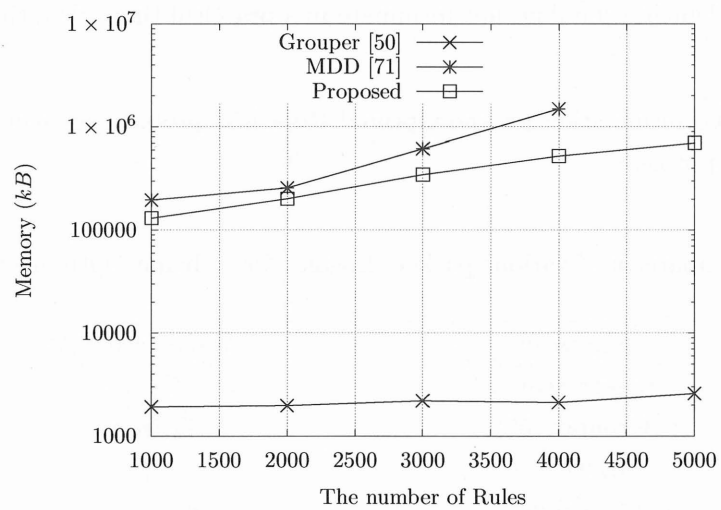


Figure 5.11: Required memory (kB).

## Chapter 6

# Conclusions

This thesis has mainly discussed two problems related to packet classification. One is an optimization problem for static early decisions and the other concerns packet classification algorithms based on software.

For the early-decision optimization problem, we identified the following issues:

1. It is necessary to develop a policy checker to ensure that the reconstructed rule list maintains the original policy.
2. ORO should take the packet arrival distribution as input and consider variations in the rule weights. This was formulated as RORO.
3. There is a problem with the pseudo-code for the state-of-the-art SGM [77] whereby its naive implementation does not terminate in a practical time when the precedence relation is dense.
4. There is no formulation for the Optimal Rule *List* problem instead of the Optimal Rule *Ordering* problem.

Table 6.1: Comparison of various packet classification schemes with arbitrary bitmask rules.

Algorithm	Worst-case Time	Worst-case Space
Linear Search	$O(nw)$	$O(nw)$
Grouper [50]	$O(tn/w)$	$O(2^{w/t} \cdot tn)$
MDD [71]	$O(w)$	$O(2^w)$
RBT Search [57]	$O(nw + w^2)$	$O(nw)$
RBT Decision Tree [57]	$O(w^2)$	$O(n^w)$
MOB [44]	$O(nw)$	$O(nw^2)$
Decision Tree constructed on RBT with pointers	$O(w)$	$O(2^w)$
Cascaded Circular-RBT	$O(kw)$	$O(nw)$

We obtain the following results for these problems:

1. We developed a policy checker using ZDDs and confirmed its effectiveness with 5000 rules.
2.
  - We showed that the problem of computing the weight for the default rule  $r_n$  with order  $\sigma$  under an uniform distribution  $U$  is  $\#\mathbf{P}$ -complete and developed an algorithm based on ZDDs for this problem.
  - We showed that RORO is  $\mathbf{NP}$ -hard.
  - We proposed a simulated annealing algorithm for RORO and confirmed its effectiveness with 500 rules.
  - We developed a pairing algorithm that pairs rules causing policy violations until there are no such rules, allowing the rules to be simply sorted according to their weights. This algorithm decreased the classification latency and reordering time compared with SGM.
  - We fixed the bug in the pseudo-code of SGM, and accelerated this algorithm by changing the representation of the precedence relation from an adjacent matrix to an adjacent list, and confirmed its effectiveness in experiments.
  - We formulated the ORL problem and developed a corresponding algorithm. This algorithm rewrites the rule list such that its graph of precedence relations becomes a forest of oriented trees, from which the order of rules can be optimized. The effectiveness of this algorithm was demonstrated through a series of experiments.

We now consider tasks for future work with regard to ORO. Although we showed that RORO is  $\#\mathbf{P}$ -complete, the computational complexity of ORL is still unclear. Because the effectiveness of the proposed algorithms was only demonstrated in experiments using the packet classification benchmark ClassBench [80], it is necessary to extend these results to the NFV environment (e.g., Open vSwitch [64]).

For the problem of packet classification based on software, we showed that it is necessary to develop a classification algorithm according to arbitrary bitmask rules, whereby the packet classification time is independent of the number of rules. In this study, we proposed an algorithm that first constructs a decision tree from RBT [57] with pointers, and then classifies packets via the decision tree. The time complexity of this algorithm is  $O(w)$ . We also developed a classification algorithm that divides a rule list into some rule lists  $\mathcal{R}_1, \mathcal{R}_2, \dots, \mathcal{R}_k$  so that every rule in  $\mathcal{R}_i$  has only circular-runs, constructs a list of CircRBTs  $\mathcal{S}_1, \mathcal{S}_2, \dots, \mathcal{S}_k$ , and classifies packets via this list. The time and space complexities of this algorithm are  $O(kw)$  and  $O(nw)$ .

There are several tasks for future work with regard to packet classification based on software. To construct the decision tree based on RBTwP, pruning the decision tree by deleting all nodes whose children point to the same node and sharing all equivalent sub-trees would be a useful development. In terms of dividing a rule list into several Circ1P rule lists, there are three tasks. First, the time complexity of dividing a rule list is  $O(n^2r)$ , which is somewhat long. Reducing this time is an important task. Second, because the effectiveness of the proposed algorithms has

only been demonstrated using ClassBench [80], it would be interesting to determine whether the number of rule lists  $k$  is independent of the number of rules  $n$  for any rule list. Finally, the effectiveness of our algorithms should be studied in a network virtualization environment, as should our algorithms for static early decisions.

# Acknowledgment

I would like to express my sincere gratitude to my supervisor, Professor Ken TANAKA. I am grateful to Dr. Kenji Mikawa from Center for Academic Information Service, Niigata University for his assistance. My sincere thanks to Professors Leo NAGAMATSU and Kazuto MATSUO from Field of Information Sciences, Graduate School of Science, Kanagawa University for their helpful comments. Finally, I would like to thank the members of TANAKA laboratory for their support.

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# Appendix A

## Simulated Annealing for RORO

In this appendix, we present a multi-start local optimization method (MSL) and a simulated annealing method for RORO [40, 41].

### A.1 Multi-Start Local Optimization (MSL)

To implement MSL, we first define a neighbor  $N(\sigma)$  for solution  $\sigma$ . In the proposed method, Eq. (A.1) is used to determine a neighbor to solution  $\sigma$ .

$$N(\sigma) = \left\{ \sigma' \mid \left| \{k \mid \sigma(k) \neq \sigma'(k)\} \right| = 2 \right\} \quad (\text{A.1})$$

$N(\sigma)$  is obtained by choosing  $i, j \in [n]$  ( $i \neq j$ ) and swapping  $\sigma(i)$  and  $\sigma(j)$ . For example,  $N(\sigma)$  for  $\sigma = (2\ 3\ 1\ 4)$  with Equation (A.1) is

$$(3\ 2\ 1\ 4), (1\ 3\ 2\ 4), (4\ 3\ 1\ 2), (2\ 1\ 3\ 4), (2\ 4\ 1\ 3), (2\ 3\ 4\ 1).$$

The proposed method randomly generates an order  $o : [|N(\sigma)|] \rightarrow [|N(\sigma)|]$  and searches for solutions in  $N(\sigma)$  in order  $o$ .

To implement MSL, we define an evaluation function  $h$  for  $\sigma$  and  $\sigma'$  as well as a neighbor. Swapping the  $i$ th rule  $j$ th rules, the set of packets defined between the  $i$ th and  $j$ th rules may vary.

After interchanging the  $i$ th and  $j$ th rules, the sets of packets decided by the  $i$ th rule  $r_{\sigma^{-1}(i)}$ ,  $j$ th rule  $r_{\sigma^{-1}(j)}$ , and  $k$ th rule  $r_{\sigma^{-1}(k)}$  ( $i+1 \leq k \leq j-1$ ) are given by Eqs. (A.3), (A.4), and (A.5), respectively, where  $\tau_{(i,j)}$  is the order that only interchanges the  $i$ th and  $j$ th elements. From the above, let the evaluation function  $h$  for solutions  $\sigma$  and  $\sigma'$  be

$$h(\sigma, \sigma') = \sum_{k=i}^j k \cdot (|E(\mathcal{R}_\sigma, k)|_F - |E(\mathcal{R}_{\sigma'}, k)|_F), \quad (\text{A.2})$$

where  $\sigma' = \tau_{(\sigma^{-1}(i), \sigma^{-1}(j))} \circ \sigma$ .

MSL with the neighbor given by Eq. (A.1) and the evaluation function in (A.2) is described in Algorithm 16. This algorithm takes rule list  $\mathcal{R}$  and a parameter  $loop$ , repeats  $loop$  to randomly generate feasible solution  $\tau$ , and returns the optimal solution.

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**Algorithm 16: Multi-Start Local Optimization**

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**input** : Rule list  $\mathcal{R}$ , Loop parameter  $loop$   
**output**: Rule Order  $\sigma$

- 1  $\sigma \leftarrow$  initial random feasible order ;
- 2  $o \leftarrow$  searching order for  $|N(\sigma)|$  ;
- 3  $i \leftarrow 0$  ;
- 4 **while**  $i < loop$  **do**
- 5      $\tau \leftarrow$  random feasible order ;
- 6     do local optimization for  $\tau$  according to  $o$  ;
- 7     **if**  $h(\sigma, \tau) < 0$  **then**  $\sigma \leftarrow \tau$ ;
- 8      $i \leftarrow i + 1$  ;

**end**

---

## A.2 Simulated Annealing

Simulated annealing takes a temperature and allows a solution to transit to a worse solution with probability  $p$  defined by the temperature and an evaluation function.

A simulated annealing algorithm for RORO is given in Algorithm 17. The algorithm utilizes neighbor  $N'(\sigma)$  when temperature  $t$  is high compared with the initial temperature  $T$  as  $T \geq \frac{100}{t}$ .  $N'(\sigma)$  is a set of solutions  $\sigma'$  whose weights do not vary in  $N(\sigma)$ . Because  $E(\mathcal{R}, i)$  is computed at every evaluation of the solution, the algorithm uses  $N'(\sigma)$  when  $t$  is high.

$$\begin{aligned} & E(\mathcal{R}_{\tau(\sigma^{-1}(i), \sigma^{-1}(j)) \circ \sigma}, \sigma^{-1}(i)) \\ &= E(\mathcal{R}_{\sigma}, \sigma^{-1}(j)) \cup (E(\mathcal{R}_{\sigma}, \sigma^{-1}(i)) \cap M(r_{\sigma^{-1}(j)})) \cup \dots \cup (E(\mathcal{R}_{\sigma}, \sigma^{-1}(j-1)) \cap M(r_{\sigma^{-1}(j)})) \end{aligned} \quad (\text{A.3})$$

$$E(\mathcal{R}_{\tau(\sigma^{-1}(i), \sigma^{-1}(j)) \circ \sigma}, \sigma^{-1}(j)) = E(\mathcal{R}_{\sigma}, \sigma^{-1}(i)) \setminus M(r_{\sigma^{-1}(i+1)}) \setminus \dots \setminus M(r_{\sigma^{-1}(j)}) \quad (\text{A.4})$$

$$\begin{aligned} & E(\mathcal{R}_{\tau(\sigma^{-1}(i), \sigma^{-1}(j)) \circ \sigma}, \sigma^{-1}(k)) \\ &= E(\mathcal{R}_{\sigma}, \sigma^{-1}(k)) \setminus M(r_{\sigma^{-1}(j)}) \cup (E(\mathcal{R}_{\sigma}, \sigma^{-1}(i)) \setminus M(r_{\sigma^{-1}(i+1)}) \setminus \dots \setminus M(r_{\sigma^{-1}(k-1)})) \cap M(r_{\sigma^{-1}(k)}) \end{aligned} \quad (\text{A.5})$$

## A.3 Experiments

To confirm the efficiency of the proposed algorithms, we implemented them in C++ under Mac OSX 10.9.5 on an Intel Core i5 1.4GHz CPU with 4 GB main memory. We generated rule lists and header lists based on the standard benchmark for packet classification Class Bench [80], and used a ZDD library [68]. To evaluate the proposed algorithms MSL and SA algorithms, we implemented the state-of-the-art rule reordering algorithm SGM [77] in C++. The latency of a given rule list for MSL, SA, and SGM is shown in Fig. A.1. Although MSL decreases the



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**Algorithm 17: Simulated Annealing**

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**input** : Rule list  $\mathcal{R}$ ,  
Initial accepted probability  $init$ ,  
Inner Loop parameter  $loop$ ,  
Temperature factor  $temp$ ,  
Freezing Parameter  $freeze$

**output**: Rule Order  $\sigma$

```
1  $\sigma \leftarrow$  initial random feasible order ;
2  $o \leftarrow$  searching order for  $|N(\sigma)|$  ;
3 choose initial temperature  $T$  so that  $init = e^{-\Delta/t}$ ;
4  $t \leftarrow T$  ;
5  $count\_out \leftarrow 0$  ;
6 while  $count\_out < freeze \cdot |N(\sigma)|$  do
7    $count\_in \leftarrow 0$  ;
8   while  $count\_in < loop \cdot |N(\sigma)|$  do
9     if  $t < \frac{T}{100}$  then get  $\sigma' \in N'(\sigma)$  according to  $o$ ;
10    else get  $\sigma' \in N(\sigma)$  according to  $o$ ;
11     $\Delta = h(\sigma, \sigma')$  ;
12    if  $\Delta \leq 0$  then  $\sigma \leftarrow \sigma'$ ,  $out\_count \leftarrow 0$ ;
13    else
14      choose a random value  $q \in [0, 1]$  ;
15      if  $q < e^{-\Delta/t}$  then  $\sigma \leftarrow \sigma'$ ;
16       $out\_count \leftarrow out\_count + 1$  ;
17    end
18     $in\_count \leftarrow in\_count + 1$  ;
19  end
20   $t \leftarrow t \cdot temp$ 
21 end
```

---

latency for the given rule list, its latency is greater than that of SA and SGM. However, in all cases, SA has the lowest latency Thus, SA is efficient for RORO.

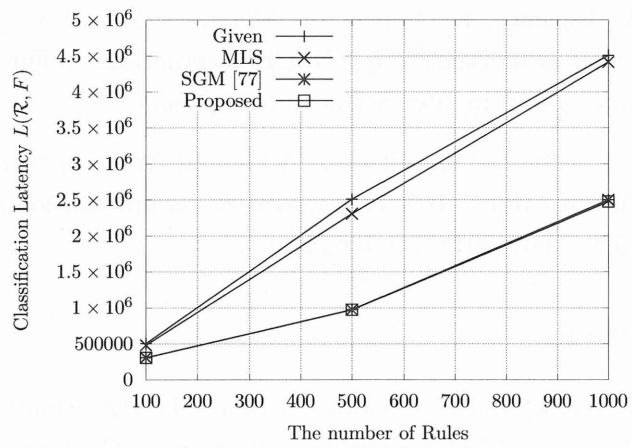


Figure A.1: Latency for rule lists with 100, 500, and 1000 rules.

# Appendix B

## Research Achievement

### B.1 Journals

1. T. Harada, Y. Ishikawa, K. Tanaka, K. Mikawa, “A Packet Classification Method via Cascaded Circular-Run-Based Trie,” *IEICE Transactions on Fundamentals of Electronics, Communications and Computer Sciences*, (to appear)
2. T. Harada, K. Tanaka and K. Mikawa, “A Method for Computing the Number of Packets Matching a Filtering Rule,” *IEICE Transactions on Information & Systems*, Vol. J101-D, No.3, pp.522-529, Mar., 2018, (in Japanese)

### B.2 Conferences

1. T. Harada, K. Tanaka and K. Mikawa, “A Heuristic Algorithm for Relaxed Optimal Rule Ordering Problem,” 2nd Cyber Security in Networking Conference (CSNet’18), Oct., 2018
2. T. Harada, K. Tanaka and K. Mikawa, “Acceleration of Packet Classification via Inclusive Rules,” *IEEE Conference on Communications and Network Security (CNS)*, pp.598-599, May, 2018

### B.3 Technical Reports

1. T. Harada, K. Tanaka, K. Mikawa, “Deciding Equivalence of The Rule List Policies via ZDD,” *IPSJ SIG Technical Reports*, Vol.2019-AL-171, No.8, pp.1-8, Jan., 2019 (in Japanese)
2. T. Fuchino, T. Harada, K. Tanaka, K. Mikawa, “A Reordering Method via Rules Pairing based on Average Weights,” *IEICE Technical Report, Circuits and Systems*, Vol.118, No.295, pp.31-36, Nov., 2018 (in Japanese)
3. T. Harada, K. Tanaka, K. Mikawa, “Packet Filter Reconstruction by Rules Encapsulation,” *IEICE Technical Report, Circuits and Systems*, Vol. 118, No.82, pp.93-98, Jun., 2018, (in Japanese)

4. T. Harada, K. Tanaka, K. Mikawa, "A Packet Classification Method for a List of Run-Based Tries Consisting of a Single Run," IPSJ SIG Technical Reports, Vol.2018-AL-167, No.3, pp.1-8, Mar. , 2018 (in Japanese)
5. T. Harada, K. Tanaka, K. Mikawa, "Heuristic Algorithms for Optimal Rule Ordering with Varying Rule Weights," IPSJ SIG Technical Reports, Vol.2018-AL-166, No.10, pp.1-8, Jan., 2018 (in Japanese)
6. T. Harada, K. Tanaka, K. Mikawa, "Computing the Number of Packets that match A Filtering Rule via MTZDDs," IEICE Technical Report, Circuits and Systems, Vol.117, No.96, pp.45-50, Jun., 2017 (in Japanese)
7. T. Harada, K. Tanaka, K. Mikawa, "An RBT Decision Tree Construction for Sparse Rules," IEICE Technical Report, Computation, Vol.117, No.28, pp.9-15, May, 2017 (in Japanese)
8. T. Harada, K. Tanaka, K. Mikawa, "A Fast Search Method for Run-Based Trie Consisting of A Single Run," IPSJ SIG Technical Reports, Vol.2017-AL-162, No.2, pp.1-7, Mar., 2017 (in Japanese)
9. T. Harada, K. Tanaka, K. Mikawa, "A Fast Search Method for Run-Based Tries via Pointers," IEICE Technical Report, Circuits and Systems, Vol. 116, No.315, pp.13-18, Nov., 2016 (in Japanese)

## B.4 Programs

<https://github.com/tanakalab>

